

Energy Transfer Phenomenon and Color-Tunable Properties of $\text{Ca}_2\text{Al}_2\text{SiO}_7$: $\text{Dy}^{3+}/\text{Eu}^{3+}$ Phosphors

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Abstract. $\text{Ca}_2\text{Al}_2\text{SiO}_7$ (CAS) doped with rare-earth ions: Eu^{3+} , Dy^{3+} , and $\text{Dy}^{3+}/\text{Eu}^{3+}$ has been successfully synthesized by the solid-phase reaction method. During the process, the sample was sintered at 1280°C within 1 hour. The energy transfer phenomenon from Dy^{3+} to Eu^{3+} was observed in the CAS matrix. Optimal doping concentrations of both rare-earth ions (Dy^{3+} , Eu^{3+}) in CAS: $\text{Dy}^{3+}/\text{Eu}^{3+}$ were determined for both Dy^{3+} (1.5 mol%) and Eu^{3+} (1.0 mol%), respectively. In addition, the energy transfer mechanism, CIE color coordinate, and CCT color temperature of CAS: $\text{Dy}^{3+}/\text{Eu}^{3+}$ were also presented and discussed.

Keywords: $\text{Ca}_2\text{Al}_2\text{SiO}_7$, $\text{Dy}^{3+}/\text{Eu}^{3+}$, energy transfer

1 Introduction

Luminescent material has brought about numerous successes in the lighting and display fields. In recent years, luminescent material on alkaline-earth aluminosilicate matrix CAS doped with rare earth or transition metal ions has attracted interest from various research groups. Thanks to its high luminescent efficiency, spectral characteristics, and suitability for many applications. In 1992, aiming to conduct research to invent material for the laser diode, Larry and collaborators issued a publication on CAS material doped with Cr^{4+} transition metal [1]. Then, studies on the luminescent properties of CAS material doped or co-doped with RE^{3+} ions (Eu^{3+} , Er^{3+} , Ce^{3+} , Tb^{3+} , etc) have been conducted [2–6]. In particular, research on absorption transition

and emission of Er^{3+} in CAS: Er^{3+} for diode laser application [3]; research on emission color manipulation and emission intensity enhancement in CAS material co-doped with Tb^{3+} , Bi^{3+} or Sm^{3+} , La^{3+} [7]; research on Energy transfer (ET) between Ce^{3+} and Tb^{3+} [5], Ce^{3+} and Mn^{2+} [8], Tm^{3+} and Dy^{3+} [9] have already been done. Therefore, we hope that the energy transfer phenomenon between Dy^{3+} and Eu^{3+} also occurs in CAS: $\text{Dy}^{3+}/\text{Eu}^{3+}$. For that reason, the paper has two purposes: (1) Study the energy transfer between two rare earth metal ions: Dy^{3+} and Eu^{3+} in CAS matrix. (2) Study the CIE color coordinate and CCT color temperature of CAS: $\text{Dy}^{3+}/\text{Eu}^{3+}$. In addition, the phase structure and luminescent characteristics of single-doped CAS: Dy^{3+} and Eu^{3+} materials are also presented and discussed.

2 Experimental

Eu³⁺ and Dy³⁺ ions doped with CAS phosphor were prepared by the solid-state reaction. Chemical reagents include CaCO₃ (99.9%, China), Al₂O₃ (99%, China), SiO₂ (99.9%, Korea), Eu₂O₃ (99.9%, Merck), and Dy₂O₃ (99.9%, Merck). These precursors are weighted by molar ratio and mixed with 4 *weight* percent B₂O₃ (used as fluxing agents). The mixtures are well ground for two hours using an agate mortar. Then the mixtures were annealed at 1280°C for 1 hour [10]. Experimental measurements such as X-ray diffraction (XRD), photoluminescence (PL), Photoluminescence excitation (PLE), and color chromaticity coordinates (CIE) were made in order to study the structural characteristic and luminescent properties of the prepared samples. XRD patterns were recorded using an x-ray diffractometer (D8Advance; Bruker, Germany). PL and PLE spectra were examined using a spectrophotometer (FL3-22; Horiba Jobin-Yvon) at room temperature.

3 Results and Discussion

3.1 Crystal structure of single-doped and co-doped CAS: Dy³⁺/Eu³⁺

The crystal structure of Ca₂Al₂SiO₇ doped with rare-earth ions and luminescent material was characterized by the X-ray diffraction method. XRD diagrams of Ca₂Al₂SiO₇: Dy³⁺ (x mol%) and Eu³⁺ (1.0 mol%) are shown in Figure 1. The analysis results indicate that the material had the desired Ca₂Al₂SiO₇ phase structure, P-42_{1m} space group, and tetragonal phase, well in accordance with the JCPDS 35-0755 standard card. The phase structure of Ca₂Al₂SiO₇ had high repetitiveness when the concentration of Dy³⁺ dopant was increased from 0 mol% to 3.5 mol%, indicating that the technological procedure has high stability and repetitiveness. On the other hand, the XRD

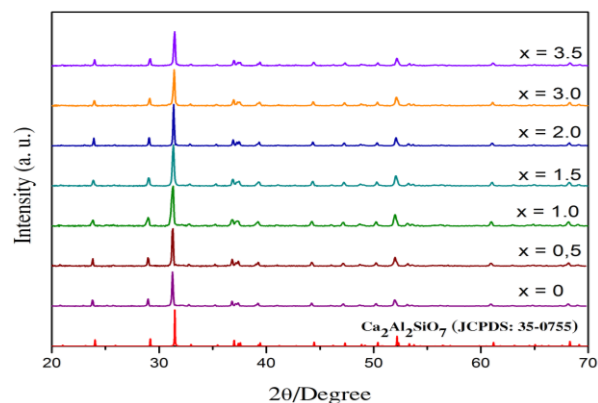


Fig. 1. The XRD diagram of CAS: Dy³⁺ (x mol%), Eu³⁺ (1.0 mol%)

diagram shows no characteristic peaks of rare-earth ions or other initial reagents. The observation proves that the small doping concentration in the matrix does not change the material's phase structure [11].

3.2 Luminescent properties of Ca₂Al₂SiO₇: Dy³⁺/Eu³⁺ phosphor

Energy transfer phenomena from Dy³⁺ to Eu³⁺ have also been detected in other matrices such as NaLa(MoO₄)₂ [12], Ca₂ZnSi₂O₇ [13], and Gd₂MoO₆ [14]. We expected that the energy transfer phenomenon from Dy³⁺ to Eu³⁺ would also occur in the CAS matrix. To determine whether ET occurs in ET or not, the following spectral characteristics were investigated: The PL spectrum of CAS: Dy³⁺ (0.5 mol%) and the PLE spectrum of CAS: Eu³⁺ (0.5 mol%) are shown in Figure 2.

The results show that the PL spectrum of Dy³⁺ overlapped with the excitation maxima of Eu³⁺ in the region from 400 to 600 nm. Notably, the relatively strong excitation emission located at 463 nm of Eu³⁺ (⁷F₀→⁵D₂) is totally within the emission band of Dy³⁺. Therefore, we predicted that ET from Dy³⁺ to Eu³⁺ could occur in the CAS matrix.

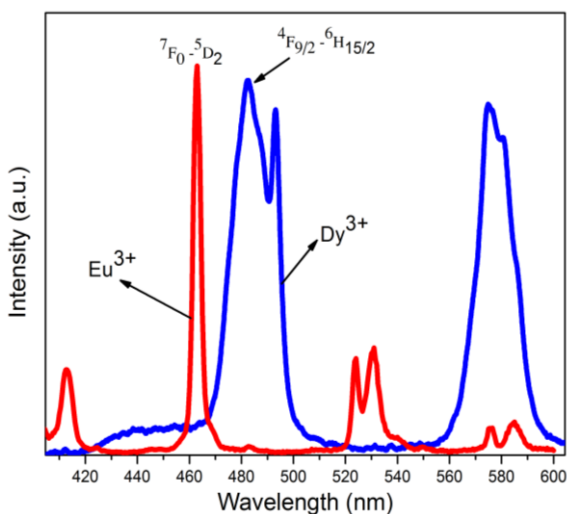


Fig. 3. PLE spectra of CAS: Eu^{3+} (0.5 mol%) ($\lambda_{\text{em}} = 617 \text{ nm}$) and PL spectra of CAS: Dy^{3+} (0.5 mol%) $\lambda_{\text{ex}}=350 \text{ nm}$.

PL spectra of CAS samples single or co-doped with Dy^{3+} and Eu^{3+} are shown in Figure 3. Both spectra were excited at a wavelength of 350 nm, taken at room temperature, in the same conditions. The spectra show that, when excited at a wavelength of 350 nm, the PL spectrum of CAS: Eu^{3+} has some narrow lines, the line at 617 nm has the highest intensity, corresponding to ${}^5D_0 \rightarrow {}^7F_2$ of Eu^{3+} ions [15-17]. However, the luminescent intensity of Eu^{3+} in CAS: Eu^{3+} is weaker than that of CAS: Dy^{3+} . The PL spectrum of CAS: Dy^{3+} has narrow lines located at 478 and 575 nm, which are the characteristic transition and emission of Dy^{3+} [18, 19], correspond to ${}^4F_{9/2} \rightarrow {}^6H_J$ ($J = 15/2, 13/2$) transitions, and have a stronger intensity than that of CAS: Eu^{3+} . The spectrum of CAS: Eu^{3+} material shows characteristic emission of both Dy^{3+} and Eu^{3+} , including narrow lines located at 478 and 575 nm, which correspond to the transition of Dy^{3+} , and a maximum located at 617 nm, which corresponds to the transition of Eu^{3+} [20]. However, the intensity of lines at 478 and 575 nm in co-doped samples is considerably smaller than that of Dy^{3+} single-doped samples. Meanwhile, the maximum emission intensity of lines corresponding to Eu^{3+} increased considerably compared to that of CAS: Eu^{3+} with the same dopant concentration. The observation shows that

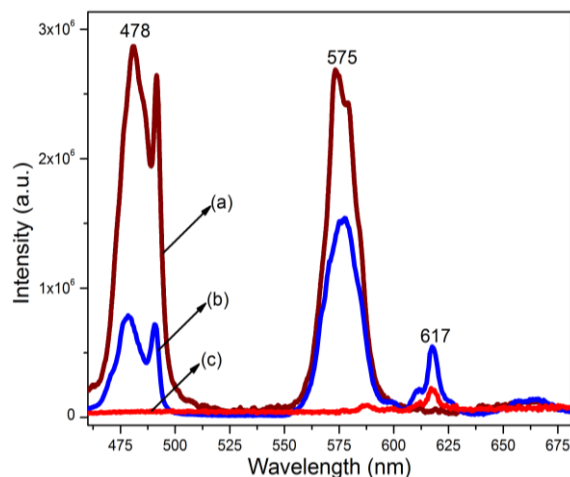


Fig. 2. PL spectra of CAS: Dy^{3+} (0.5 mol%) (a), PL spectra of CAS: Dy^{3+} (0.5 mol%), Eu^{3+} (1.0 mol%) (b) and PL spectra of CAS: Eu^{3+} (1.0 mol%) (c), $\lambda_{\text{ex}}=350 \text{ nm}$

energy transfer from Dy^{3+} to Eu^{3+} could occur in the CAS matrix.

The PLE spectra of CAS: Eu^{3+} (1,0 mol%), excited at a wavelength of 617 nm; CAS: Dy^{3+} (0,5 mol%), excited at a wavelength of 575 nm and CAS: Eu^{3+} (1,0 mol%); and Dy^{3+} (0,5 mol%), excited at a wavelength of 617 nm are shown in Figure 4. The spectrum shows that the excitation transition of Eu^{3+} that causes the characteristic peak of Eu^{3+} in CAS: Eu^{3+} has low intensity, narrow lines with maxima located at 360, 374, 380, 393, and 412 nm. Besides, the PLE spectrum of CAS: Dy^{3+} has high intensity, narrow lines with maxima located at 322, 350, 363, 383, 425, and 451 nm. Meanwhile, the PLE spectrum of CAS: $\text{Dy}^{3+}/\text{Eu}^{3+}$ corresponds to a peak at 617 nm of Eu^{3+} and has a similar shape to the PLE spectrum of Eu^{3+} , plus a few minor transitions due to the contribution of Dy^{3+} . The contribution to the direct stimulation of Eu^{3+} is very small, mainly due to the absorption of Dy^{3+} ions, to generate emission of Dy^{3+} through ET between Dy^{3+} and Eu^{3+} . The observation shows that the emission efficiency of Eu^{3+} is relatively high when co-doped with Dy^{3+} in the CAS matrix.

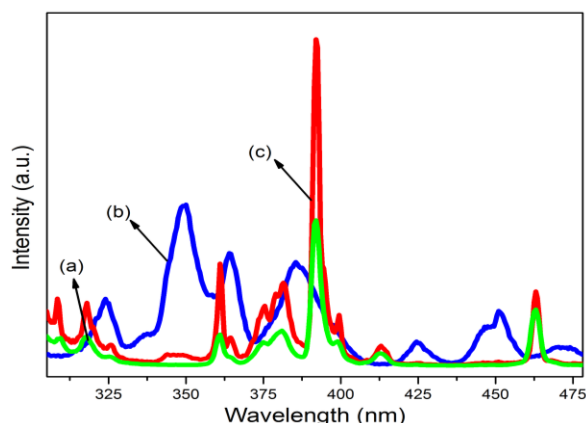


Fig. 4. PLE spectra of CAS: Eu³⁺ (1.0 mol%) with ($\lambda_{em} = 617$ nm) (a), CAS: Dy³⁺ (0.5 mol%) with ($\lambda_{em} = 575$ nm) (b), CAS: Dy³⁺ (0.5 mol%), Eu³⁺ (1.0 mol%) with ($\lambda_{em} = 617$ nm) (c)

To further clarify the ET mechanism from Dy³⁺ to Eu³⁺ in CAS: Dy³⁺/Eu³⁺, we studied the PL spectra of the CAS: Dy³⁺ (x mol%), and Eu³⁺ (1.0 mol%), stimulated at 350 nm. All spectra were taken at room temperature with the same measuring conditions (Figure 5). The result shows that, when the sample is not co-doped with Dy³⁺, the emission intensity of CAS: Eu³⁺ is very weak, and only characteristic emission of Eu³⁺ in the matrix is observed. As the doping concentration of Dy³⁺ increased from 0,5 – 3,5 mol%, the position of the emission maximum of both Eu³⁺ and Dy³⁺ in the PL spectrum remained unchanged, while the emission intensity of both ions increased. The phenomenon showed that, although the concentration of Eu³⁺ ions remained unchanged, their emission intensity increased as the doping concentration of Dy³⁺ increased. The result further confirmed the occurrence of ET from Dy³⁺ to Eu³⁺ ions in the CAS matrix. Besides, Figure 6 shows the PLE spectra of CAS: Dy³⁺ (x mol%), Eu³⁺ (1.0 mol%) excited at a wavelength of 617 nm. As the doping concentration of Dy³⁺ increased, the shape of the PLE spectra remained unchanged, but the emission intensity changed. The PLE spectra of the co-dope sample still have a peak at 350 nm, which corresponds to the absorption of Dy³⁺ ions.

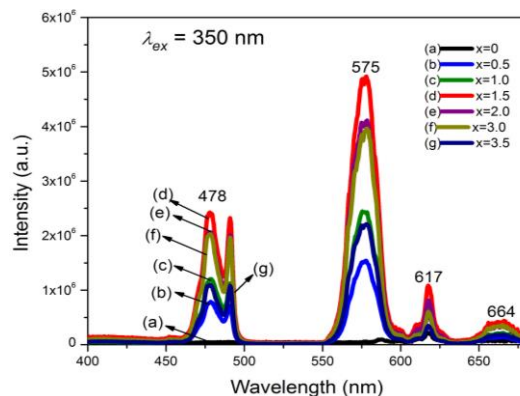


Fig. 5. PL Spectra of CAS: Dy³⁺ (x mol%), Eu³⁺ (1.0 mol%), $\lambda_{ex} = 350$ nm

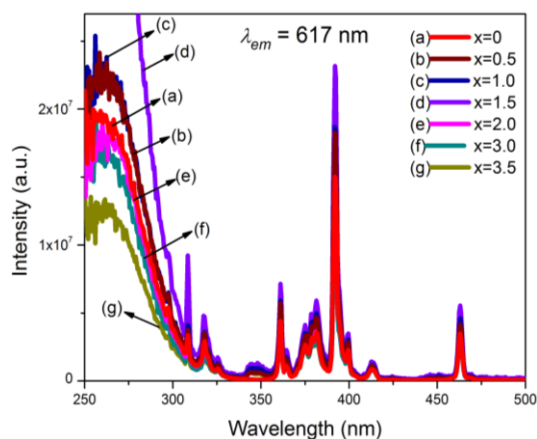


Fig. 6. PLE Spectra of CAS: Dy³⁺ (x mol%), Eu³⁺ (1.0 mol%), $\lambda_{em} = 617$ nm

The mechanism of energy transfer from Dy³⁺ to Eu³⁺ ions in the CAS matrix is shown in Figure 7, based on the energy diagram of Dy³⁺ and Eu³⁺ ions. When being stimulated by a wavelength of 350 nm, electrons of Dy³⁺ transit from the ⁶H_{15/2} ground state to the ⁶P_{7/2} excited state, then electrons transit to the lowest excited state ⁴F_{9/2} of Dy³⁺, before transiting to the ⁶H_{*J*} ground state (with $J = 15/2, 13/2, 11/2$), emitting narrow lines with maxima located at 478, 575, and 664 nm. Simultaneously, part of the excitation energy of Dy³⁺ is transferred to Eu³⁺, causing it to transit to an excited state followed by a non-emission to ⁵D₀ low excited states before transiting to ⁷F_{*J*} ground state, emitting narrowly lined characteristics peaks of Eu³⁺.

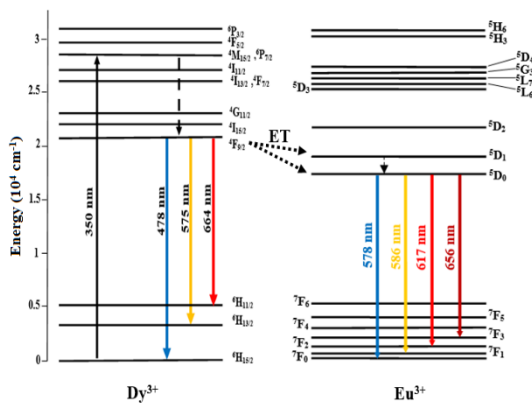


Fig. 7. Energy transfer mechanism from Dy³⁺ ion to Eu³⁺ ion in CAS

In order to study the influence of energy transfer from Dy³⁺ to Eu³⁺ in the CAS matrix, the dependence of the intensity of characteristic emission of Dy³⁺ and Eu³⁺ ions in CAS: Dy³⁺ (*x* mol%) and Eu³⁺ (1,0 mol%) samples on the doping concentration of Dy³⁺ ions is shown in Figure 8. The result shows that the emission intensity corresponds to the wavelengths 478 and 575 nm of Dy³⁺ and 617 nm of Eu³⁺ and increases when the doping concentration of Dy³⁺ increases, reaching its maximum when the doping concentration of Dy³⁺ reaches 1.5%/mol. Beyond this value, the maximum luminescent intensity of both Dy³⁺ and Eu³⁺ decreases, the decrease is because of the concentration quenching phenomenon.

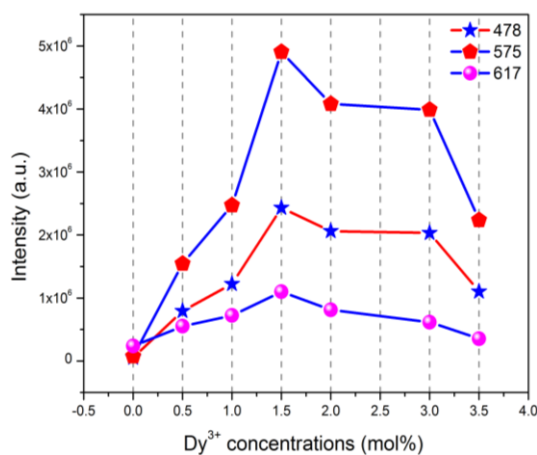


Fig. 8. The dependence of PL intensity (peak at 478 nm, 575 nm and 617 nm) on the concentration of Dy³⁺ ion

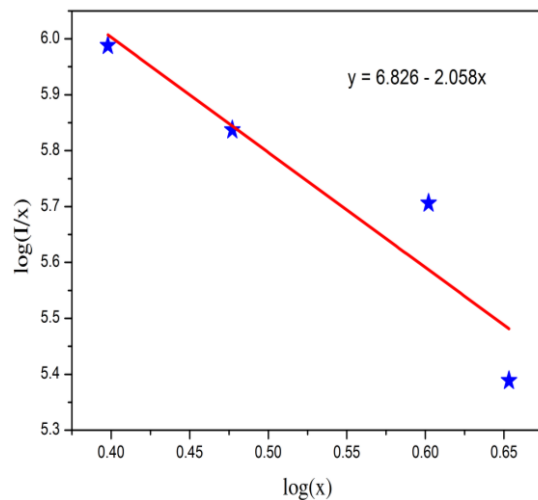


Fig. 9. The relation between $\log(I/x)$ and $\log(x)$ of CAS: Dy³⁺/Eu³⁺

According to the theory of dopant concentration quenching of Dexter and Blasse, the concentration quenching ET critical distance between Dy³⁺ and Eu³⁺ is given by the following equation (1) [21-23].

$$R_c = 2 \left(\frac{3V}{4\pi x_c N} \right)^{1/3}, \quad (1)$$

where x_c is the total concentration of Dy³⁺ and Eu³⁺ ions at which the quenching begins to occur, N is the number of cations in an unit cell, V is the volume of the unit cell. From the PL spectral data of CAS: Dy³⁺ (*x* mol%) and Eu³⁺ (1.0 mol%), we have calculated and determined that $V = 299.39 \text{ \AA}^3$, $N = 2$ [6], and the concentration at which the intensity quenching begins to occur is Eu³⁺ = 1.0 mol% and Dy³⁺ = 1.5 mol% in CAS: Dy³⁺/Eu³⁺. Substituting these values to equation (1), we obtain the ET critical distance between Dy³⁺ and Eu³⁺ was 22.53 Å. The distance is rather large, therefore, the luminescent intensity concentration quenching caused by multipolar interaction is used to explain the phenomenon in material containing two type's emission center. The graphs of $\log(I/x)$ with $\log(x)$ of CAS: Dy³⁺/Eu³⁺ correspond to different concentrations of Dy³⁺ and are shown in Figure 9. From the graph, the slope for CAS:

Dy^{3+}/Eu^{3+} is determined to be -2.058 and Q is calculated to be 6.174, very close to 6. The result showed that d-d interaction is the main contributor to luminescent intensity dopant concentration quenching of Dy^{3+} and Eu^{3+} in CAS: Dy^{3+}/Eu^{3+} .

3.3 Color chromaticity coordinates of CAS: Dy^{3+}/Eu^{3+} phosphors

As we know, CIE color coordinates are usually used to assess the particular applicability of luminescent material [24-27]. For CAS: Dy^{3+}/Eu^{3+} , stimulated at 350 nm, the color coordinate value of CAS: Dy^{3+}/Eu^{3+} could be changed by adjusting the concentration of Dy^{3+} . The color coordinate of CAS: Eu^{3+} (1.0 mol%) is in the red region, while that of CAS: Dy^{3+} (0.5 mol%) is in the whitish yellow region. The co-doping of Dy^{3+} with CAS: Eu^{3+} causes a color coordinate shift toward the orange direction (Figure 10).

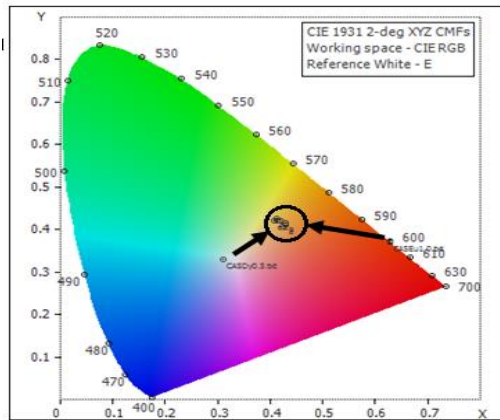


Fig. 10. CIE Color coordinate of the CAS: Dy^{3+} (x mol%), Eu^{3+} (1.0 mol%) samples when being stimulated by a wavelength at 350 nm

3.4 Correlated color temperature of CAS: Dy^{3+}/Eu^{3+} phosphors

The calculated CIE (the Commission International de l'Éclairage) chromaticity coordinates of CAS: Dy^{3+}/Eu^{3+} phosphors from the emission spectra are shown in Fig. 10. The x and y color chromaticity coordinates of CAS: Dy^{3+}/Eu^{3+} phosphors were

used to calculate the correlated color temperature (CCT) by using McCamy's relation [24-26].

$$CCT = -449n^3 + 3525n^2 - 6823n + 5520.33, \quad (2)$$

where $n = (x - x_e)/(y - y_e)$ is the inverse slope line and $(x_e = 0.332, y_e = 0.186)$ indicates the isotemperature lines' epicenter [25]. The color chromaticity coordinates and CCT values of CAS: Dy^{3+}/Eu^{3+} phosphors with various Dy^{3+}/Eu^{3+} ions concentrations are listed in Table I. The results from Fig. 10 and Table I show that the color chromaticity coordinates are in the red region and have slight differences with various Dy^{3+}/Eu^{3+} ions concentrations. The CCT values of the prepared samples increase slightly as Dy^{3+} concentrations increase, and their temperature corresponds to 'Warm White' light in human visual perception [28].

Table 1. Color chromaticity coordinates (x, y) and CCT of CAS: Dy^{3+}/Eu^{3+} materials.

Samples	x	y	CCT (K)
CAS: Eu^{3+} (1.0 mol%)	0.629	0.370	1803
CAS: Dy^{3+} (0.5 mol%)	0.311	0.330	6591
CAS: Dy^{3+} (0.5 mol%), Eu^{3+} (1.0 mol%)	0.429	0.412	3206
CAS: Dy^{3+} (1.0 mol%), Eu^{3+} (1.0 mol%)	0.430	0.416	3218
CAS: Dy^{3+} (1.5 mol%), Eu^{3+} (1.0 mol%)	0.418	0.420	3467
CAS: Dy^{3+} (2.0 mol%), Eu^{3+} (1.0 mol%)	0.415	0.421	3530
CAS: Dy^{3+} (3.0 mol%), Eu^{3+} (1.0 mol%)	0.407	0.421	3687
CAS: Dy^{3+} (3.5 mol%), Eu^{3+} (1.0 mol%)	0.412	0.427	3627

4 Conclusions

Studying the PL and PLE spectra of CAS: (x mol%) Dy^{3+} , (1.0 mol%) Eu^{3+} , samples with $x = 0$; 0.5; 1.0; 1.5; 2.0; 3.0; 3.5, we found out that the optimal doping concentration of Dy^{3+} was 1,5mol%, at which the maximum luminescent intensity was obtained. In addition, energy transfer from Dy^{3+} to Eu^{3+} phenomenon was observed in the CAS matrix; d-d interaction is the main contributor to luminescent intensity dopant concentration quenching of Dy^{3+} and Eu^{3+} in CAS: Dy^{3+}/Eu^{3+} . Luminescent color temperature of CAS: Dy^{3+}/Eu^{3+} co-doped material when excited at a wavelength of 350 nm was within 3200 - 3700K; the CIE color coordinate shows that the material emitted orange radiation, suitable for developing LED in lighting technology.

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